



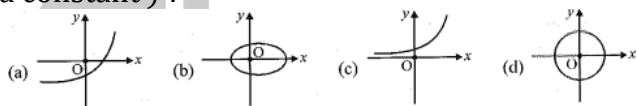
# D PHYSICS

CSIR-NET,GATE , ALL SET, JEST, IIT-JAM, BARC

Contact: 8830156303 | 7741947669

❖ CSIR-UGC-NET/JRF- JUNE – 2018 PHYSICAL SCIENCES BOOKLET - [A]

➤ PART-B

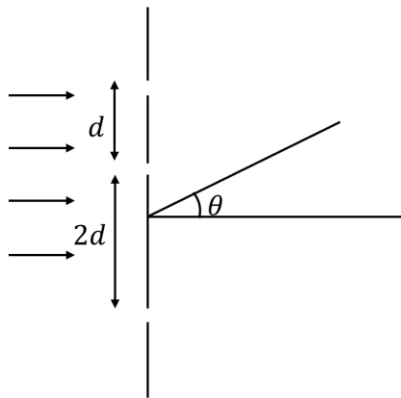
- Consider the three vectors  $\vec{v}_1 = 2\hat{i} + 3\hat{k}$ ,  $\vec{v}_2 = \hat{i} + 2\hat{j} + 2\hat{k}$  and  $\vec{v}_3 = 5\hat{i} + \hat{j} + \alpha\hat{k}$ , where  $\hat{i}$ ,  $\hat{j}$  and  $\hat{k}$  are the standard unit vectors in a three-dimensional Euclidean space. These vectors will be linearly dependent if the value of  $\alpha$  is  
(a) 31/4 (b) 23/4  
(c) 27/4 (d) 0
- The fourier transform  $\int_{-\infty}^{\infty} dx f(x) e^{ikx}$  of the function  $f(x) = e^{-|x|}$  is  
(a)  $-\frac{2}{1+k^2}$  (b)  $-\frac{1}{2(1+k^2)}$   
(c)  $\frac{2}{1+k^2}$  (d)  $\frac{2}{(2+k^2)}$
- The value of the integral  $\int_{-\pi/2}^{+\pi/2} dx \int_{-1}^{+1} dy \delta(\sin 2x) \delta(x-y)$  is  
(a) 0 (b) 1/2  
(c)  $1/\sqrt{2}$  (d) 1
- Consider the following ordinary differential equation :  $\frac{d^2x}{dt^2} + \frac{1}{x} \left(\frac{dx}{dt}\right)^2 - \frac{dx}{dt} = 0$  with the boundary conditions  $x(t=0) = 0$  and  $x(t=1) = 1$ . The value of  $x(t)$  at  $t$  is  
(a)  $\sqrt{e-1}$  (b)  $\sqrt{e^2+1}$   
(c)  $\sqrt{e+1}$  (d)  $\sqrt{e^2-1}$
- What is the value of  $\alpha$  for which  $f(x,y) = 2x + 3(x^2 - y^2) + 2i(3xy + \alpha y)$  is an analytic function of complex variable  $z = x + iy$ ?  
(a) 1 (b) 0
- A particle moves in the one-dimensional potential  $V(x) = \alpha x^6$ , where  $\alpha > 0$  is a constant. If the total energy of the particle is  $E$ , its time period in a periodic motion is proportional to  
(a)  $E^{-1/3}$  (b)  $E^{-1/2}$   
(c)  $E^{1/3}$  (d)  $E^{1/2}$
- Which of the following figures best describes the trajectory of a particle moving in a repulsive central potential  $V(r) = \frac{\alpha}{r}$  ( $\alpha > 0$  is a constant) ?  

- Two particles A and B move with relativistic velocities of equal magnitude  $v$ , but in opposite directions, along the  $x$ -axis of an inertial frame of reference. The magnitude of the velocity of A, as seen from the rest frame of B, is  
(a)  $\frac{2v}{(1-\frac{v^2}{c^2})}$  (b)  $\frac{2v}{(1+\frac{v^2}{c^2})}$   
(c)  $2v \sqrt{\frac{c-v}{c+v}}$  (d)  $\frac{2v}{\sqrt{1-\frac{v^2}{c^2}}}$
- A particle of mass  $m$ , kept in a potential  $V(x) = -\frac{1}{2}kx^2 + \frac{1}{4}\lambda x^4$ , [where  $k$  and  $\lambda$  are positive constants], undergoes small oscillations about an equilibrium point. The frequency of oscillations is

(a)  $\frac{1}{2\pi} \sqrt{\frac{2\lambda}{m}}$   
 (c)  $\frac{1}{2\pi} \sqrt{\frac{2k}{m}}$

(b)  $\frac{1}{2\pi} \sqrt{\frac{k}{m}}$   
 (d)  $\frac{1}{2\pi} \sqrt{\frac{\lambda}{m}}$

10. Two point charges  $+2Q$  and  $-Q$  are kept at points with Cartesian coordinates  $(1,0,0)$  and  $(2,0,0)$ , respectively, in front of an infinite grounded conducting plate at  $x = 0$ . The potential at  $(x,0,0)$  for  $x \geq 1$  depends on  $x$  as  
 (a)  $x^{-3}$  (b)  $x^{-5}$   
 (c)  $x^{-2}$  (d)  $x^{-4}$

11. The following configuration of three identical narrow slits are illuminated by monochromatic light of wavelength  $\lambda$  (as shown in the figure below). The intensity is measured at angle  $\theta$  (where  $\theta$  is the angle with the incident beam) at a large distance from the slits. If  $\delta = \frac{2\pi d}{\lambda} \sin \theta$ , the intensity is proportional to



- (a)  $2\cos \delta + 2\cos 2\delta$   
 (b)  $3 + \frac{1}{8^2} \sin^2 3\delta$   
 (c)  $3 + 2\cos \delta + 2\cos 2\delta + 2\cos 3\delta$   
 (d)  $2 + \frac{1}{\delta^2} \sin^2 3\delta$

12. The electric field of a plane wave in a conducting medium is given by

$$\vec{E}(z,t) = \hat{i} E_0 e^{-s/\sqrt{3}a} \cos \left( \frac{z}{\sqrt{3}a} - \omega t \right)$$

where  $\omega$  is the angular frequency and  $a > 0$  is a constant. The phase difference between the magnetic field  $\vec{B}$  and the electric field  $\vec{E}$  is

- (a)  $30^\circ$  and  $\vec{E}$  lags behind  $\vec{B}$   
 (b)  $30^\circ$  and  $\vec{B}$  lags behind  $\vec{E}$   
 (c)  $60^\circ$  and  $\vec{E}$  lags behind  $\vec{B}$   
 (d)  $60^\circ$  and  $\vec{B}$  lags behind  $\vec{E}$

13. The electric field  $\vec{E}$  and the magnetic field  $\vec{B}$  corresponding to the scalar and vector potentials,  $V(x,y,z,t) = 0$  and  $\vec{A}(x,y,z,t) = \frac{1}{2} \hat{k} \mu_0 A_0 (ct - x)$ , where  $A_0$  is a constant, are  
 (a)  $\vec{E} = 0$  and  $\vec{B} = \frac{1}{2} \hat{j} \mu_0 A_0$   
 (b)  $\vec{E} = -\frac{1}{2} \hat{k} \mu_0 A_0 c$  and  $\vec{B} = \frac{1}{2} \hat{j} \mu_0 A_0$   
 (c)  $\vec{E} = 0$  and  $\vec{B} = -\frac{1}{2} \hat{i} \cdot \mu_0 A_0$   
 (d)  $\vec{E} = \frac{1}{2} \hat{k} \mu_0 A_0 c$  and  $\vec{B} = -\frac{1}{2} \hat{i} \mu_0 A_0$

14. A particle of mass  $m$  is confined in a three-dimensional box by the potential

$$V(x,y,z) = \begin{cases} 0, & 0 \leq x,y,z \leq a \\ \infty, & \text{otherwise} \end{cases}$$

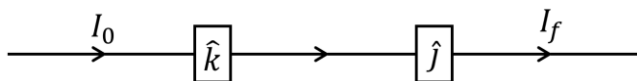
The number of eigenstates of Hamiltonian with energy  $\frac{9\hbar^2\pi^2}{2ma^2}$  is

- (a) 1 (b) 6  
 (c) 3 (d) 4

15. The Hamiltonian of a spin- $\frac{1}{2}$  particle in a magnetic field  $\vec{B}$  is given by  $H = -\mu \vec{B} \cdot \vec{\sigma}$ , where  $\mu$  is a real constant and  $\vec{\sigma} = (\sigma_x, \sigma_y, \sigma_z)$  are the Pauli spin matrices. If  $\vec{B} = (B_0, B_0, 0)$  and the spin state at time  $t = 0$  is an eigenstate of  $\sigma_x$ , then of the expectation values  $\langle \sigma_x \rangle$ ,  $\langle \sigma_y \rangle$  and  $\langle \sigma_z \rangle$   
 (a) Only  $\langle \sigma_x \rangle$  changes with time  
 (b) Only  $\langle \sigma_y \rangle$  changes with time  
 (c) Only  $\langle \sigma_z \rangle$  changes with time  
 (d) All three change with time

16. Two Stern-Gerlach apparatus  $S_1$  and  $S_2$  are kept in a line ( $x$ -axis). The directions of their magnetic fields are along the positive  $z$ - and  $y$ -axes, respectively. Each apparatus only transmits particles with spins aligned in the direction of its magnetic field. If an initially unpolarized beam of spin- $\frac{1}{2}$  particles passes through this configuration, the ratio of

intensities  $I_0$ :  $I_f$  of the initial and final beams, is



- (a) 16: 1
- (b) 2: 1
- (c) 4: 1
- (d) 1: 0

17. A particle of mass  $m$  is constrained to move in a circular ring to radius  $R$ . When a perturbation

$$V' = \frac{a}{R^2} \cos^2 \phi$$

(where  $a$  is a real constant) is added, the shift in energy of the ground state, to first order in  $a$ , is

- (a)  $a/R^2$
- (b)  $2a/R^2$
- (c)  $a/(2R^2)$
- (d)  $d/(\pi R^2)$

18. Which of the following statements concerning the coefficient of volume expansion  $\alpha$  and the isothermal compressibility  $\kappa$  of a solid is true ?

- (a)  $\alpha$  and  $\kappa$  are both intensive variables.
- (b)  $\alpha$  is an intensive and  $k$  is an extensive variable.
- (c)  $\alpha$  is an extensive and  $\kappa$  is an intensive variable.
- (d)  $\alpha$  and  $k$  are both extensive variables.

19. The van der Waals equation for one mole of a gas is  $(p + \frac{a}{V^2})(V - b) = RT$ . The corresponding equation of state for  $n$  moles of this gas at pressure  $p$ , volume  $V$  and temperature  $T$ , is

- (a)  $(p + \frac{an^2}{V^2})(V - nb) = nRT$
- (b)  $(p + \frac{a}{V^2})(V - nb) = nRT$
- (c)  $(p + \frac{an^2}{V^2})(V - nb) = RT$
- (d)  $(p + \frac{a}{V^2})(V - nb) = RT$

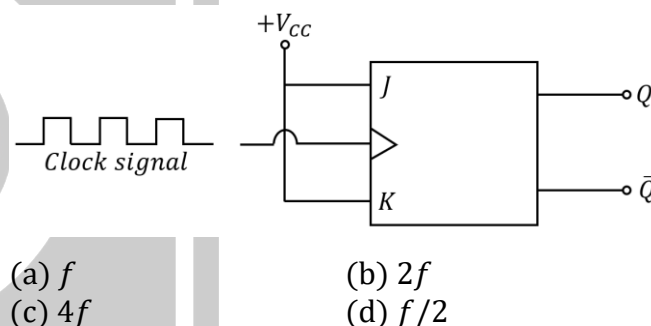
20. The number of ways of distributing 11 indistinguishable bosons in 3 different energy levels is

- (a)  $3^{11}$
- (b)  $11^3$
- (c)  $\frac{(13)!}{2!(11)!}$
- (d)  $\frac{(11)!}{3!8!}$

21. In a system of  $N$  distinguishable particles, each particle can be in one of two states with energies 0 and  $-E$ , respectively. The mean energy of the system at temperature  $T$ , is

- (a)  $-\frac{1}{2}N(1 + e^{E/k_B T})$
- (b)  $-\frac{NE}{(1 + e^{E/k_B T})}$
- (c)  $-\frac{1}{2}NE$
- (d)  $-\frac{NE}{(1 + e^{-E/k_B T})}$

22. In the following JK flip-flop circuit, J and K inputs are tied together to  $+V_{CC}$ . If the input is a clock signal of frequency  $f$ , the frequency of the output  $Q$  is

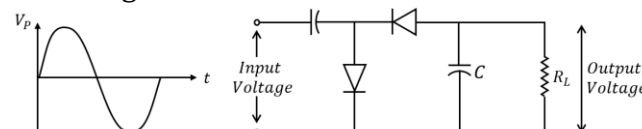


- (a)  $f$
- (b)  $2f$
- (c)  $4f$
- (d)  $f/2$

23. Which of the following gates can be used as a parity checker ?

- (a) an OR gate
- (b) a NOR gate
- (c) an exclusive OR (XOR) gate
- (d) an AND gate

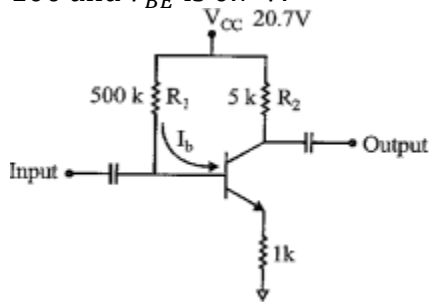
24. A sinusoidal signal with a peak voltage  $V_p$  and average value zero, is an input to the following circuit.



Assuming ideal diodes, the peak value of the output voltage across the load resistor  $R_L$ , is

- (a)  $V_p$
- (b)  $V_p/2$
- (c)  $2V_p$
- (d)  $\sqrt{2}V_p$

25. In the following circuit, the value of the common-emitter forward current amplification factor  $\beta$  for the transistor is 100 and  $V_{BE}$  is 0.7 V.



The base current  $I_B$  is

- (a)  $40\mu\text{A}$  (b)  $30\mu\text{A}$   
(c)  $44\mu\text{A}$  (d)  $33\mu\text{A}$

### ➤ PART - C

26. In the function  $P_n(x)e^{-x^2}$  of a real variable  $x$ ,  $P_n(x)$  is a polynomial of degree  $n$ . The maximum number of extrema that this function can have is

- (a)  $n + 2$  (b)  $n - 1$   
(c)  $n + 1$  (d)  $n$

27. The Green's function  $G(x, x')$  for the equation  $\frac{d^2 y(x)}{dx^2} + y(x) = f(x)$ , with the boundary values  $y(0) = y(\frac{\pi}{2}) = 0$ , is

(a)  $G(x, x') = \begin{cases} x(x' - \frac{\pi}{2}), & 0 < x < x' < \frac{\pi}{2} \\ (x - \frac{\pi}{2}), & 0 < x' < x < \frac{\pi}{2} \end{cases}$

(b)  $G(x, x') = \begin{cases} -\cos x' \sin x, & 0 < x < x' < \frac{\pi}{2} \\ -\sin x' \cos x, & 0 < x' < x < \frac{\pi}{2} \end{cases}$

(c)  $G(x, x') = \begin{cases} \cos x' \sin x, & 0 < x < x' < \frac{\pi}{2} \\ \sin x' \cos x, & 0 < x' < x < \frac{\pi}{2} \end{cases}$

(d)  $G(x, x') = \begin{cases} x(\frac{\pi}{2} - x'), & 0 < x < x' < \frac{\pi}{2} \\ x'(\frac{\pi}{2} - x), & 0 < x' < x < \frac{\pi}{2} \end{cases}$

28. The fractional error in estimating the integral  $\int_0^1 x dx$  using Simpson's  $\frac{1}{3}$ -rule, using a step

size 0.1, is nearest to

- (a)  $10^{-4}$  (b) 0  
(c)  $10^{-2}$  (d)  $3 \times 10^{-4}$

29. Which of the following statements is true for a  $3 \times 3$  real orthogonal matrix with determinant +1 ?

- (a) the modulus of each of its eigenvalues need not be 1, but their product must be 1.  
(b) at least one of its eigenvalues is +1.  
(c) all of its eigenvalues must be real.  
(d) none of its eigenvalues need be real.

30. A particle of mass  $m$  moves in a central potential  $V(r) = -\frac{k}{r}$  in an elliptic orbit

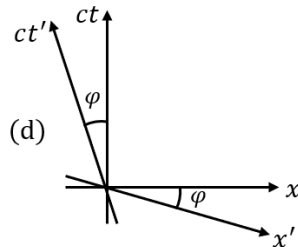
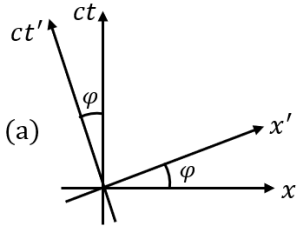
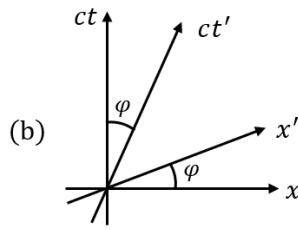
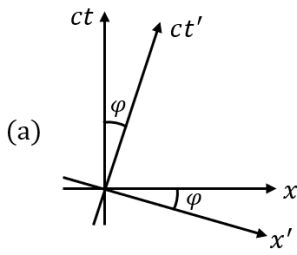
$r(\theta) = \frac{a(1-e^2)}{1+e\cos\theta}$ , where  $0 \leq \theta \leq 2\pi$  and  $a$  and  $e$  denote the semi-major axis and eccentricity, respectively. If its total energy is  $E = -\frac{k}{2a}$ , the maximum kinetic energy is

- (a)  $E(1 - e^2)$  (b)  $E \frac{(e+1)}{(e-1)}$   
(c)  $\frac{E}{(1-e^2)}$  (d)  $E \frac{(1-e)}{(1+e)}$

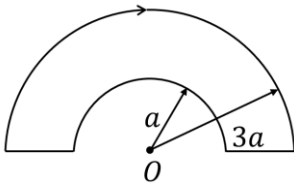
31. The Hamiltonian of a one-dimensional system is  $H = \frac{xp^2}{2m} + \frac{1}{2}kx$ , where  $m$  and  $k$  are positive constants. The corresponding Euler-Lagrange equation for the system is

- (a)  $m\ddot{x} + k = 0$   
(b)  $m\ddot{x} + 2\dot{x} + kx^2 = 0$   
(c)  $2mx\ddot{x} - m\dot{x}^2 + kx^2 = 0$   
(d)  $mx\ddot{x} - 2m\dot{x}^2 + kx^2 = 0$

32. An inertial frame  $K'$  moves with a constant speed  $v$  with respect to another inertial frame  $K$  along their common  $x$ -axis in the positive  $x$ -direction. Let  $(x, ct)$  and  $(x', ct')$  denote the space-time coordinates in the frame  $K$  and  $K'$ , respectively. Which of the following space-time diagrams correctly describes the  $t'$ -axis ( $x' = 0$  line) and the  $x'$ -axis ( $t' = 0$  line) in the  $x - ct$  plane? (In the following figures  $\tan \phi = v/c$ ).



33. The loop shown in the figure below carries a steady current  $I$ . The magnitude of the magnetic field at the point  $O$  is



- (a)  $\frac{\mu_0 I}{2a}$   
 (b)  $\frac{\mu_0 I}{6a}$   
 (c)  $\frac{\mu_0 I}{4a}$   
 (d)  $\frac{\mu_0 I}{3a}$

34. In the region far from a source, the time dependent electric field at a point  $(r, \theta, \phi)$  is

$$\vec{E}(r, \theta, \phi) = \hat{\phi} E_0 \omega^2 \left( \frac{\sin \theta}{r} \right) \cos \left[ \omega \left( t - \frac{r}{c} \right) \right]$$

where  $\omega$  is angular frequency of the source. The total power radiated (average over a cycle) is

- (a)  $\frac{2\pi E_0^2 \omega^4}{3 \mu_0 c}$   
 (b)  $\frac{4\pi E_0^2 \omega^4}{3 \mu_0 c}$   
 (c)  $\frac{4 E_0^2 \omega^4}{3\pi \mu_0 c}$   
 (d)  $\frac{2 E_0^2 \omega^4}{3 \mu_0 c}$

35. A hollow waveguide supports transverse electric (TE) modes with the dispersion relation  $k = \frac{1}{c} \sqrt{\omega^2 - \omega_{mn}^2}$ , where  $\omega_{mn}$  is the mode frequency. The speed of flow of electromagnetic energy at the mode frequency is

- (a)  $c$   
 (b)  $\omega_{mn}/k$   
 (c)  $0$   
 (d)  $\infty$

36. The energy of a free relativistic particle is  $E = \sqrt{|\vec{p}|^2 c^2 + m^2 c^4}$ , where  $m$  is its rest mass,  $\vec{p}$  is its momentum and  $c$  is the speed of light in vacuum. The ratio  $v_g/v_p$  of the group velocity  $v_g$  of a quantum mechanical wave packet (describing this particle) to the phase velocity  $v_p$  is

- (a)  $|\vec{p}|c/E$   
 (b)  $|\vec{p}|mc^3/E^2$   
 (c)  $|\vec{p}|^2 c^2/E^2$   
 (d)  $|\vec{p}|c/2E$

37. The  $n$ -th energy eigenvalue  $E_n$  of a one-dimensional Hamiltonian  $H = \frac{p^2}{2m} + \lambda x^4$ , (where  $\lambda > 0$  is a constant) in the WKB approximation, is proportional to

- (a)  $\left(n + \frac{1}{2}\right)^{4/3} \lambda^{1/3}$   
 (b)  $\left(n + \frac{1}{2}\right)^{4/3} \lambda^{2/3}$   
 (c)  $\left(n + \frac{1}{2}\right)^{5/3} \lambda^{1/3}$   
 (d)  $\left(n + \frac{1}{2}\right)^{5/3} \lambda^{2/3}$

38. The differential scattering cross section  $d\sigma/d\Omega$  for the central potential  $V(r) = \frac{\beta}{r} e^{-\mu r}$ , where  $\beta$  and  $\mu$  are positive constants, is calculated in the first Born approximation. Its dependence on the scattering angle  $\theta$  is proportional to ( $A$  is a constant below).

- (a)  $\left(A^2 + \sin^2 \frac{\theta}{2}\right)^{-1}$   
 (b)  $\left(A^2 + \sin^2 \frac{\theta}{2}\right)^{-1}$   
 (c)  $\left(A^2 + \sin^2 \frac{\theta}{2}\right)^{-2}$   
 (d)  $\left(A^2 + \sin^2 \frac{\theta}{2}\right)^2$

39. At  $t = 0$ , the wavefunction of an otherwise free particle confined between two infinite walls at  $x = 0$  and  $x = L$  is

$$\psi(x, t = 0) = \sqrt{\frac{2}{L}} \left( \sin \frac{\pi x}{L} - \sin \frac{3\pi x}{L} \right).$$

Its wavefunction at a later time  $t = \frac{mL^2}{4\pi\hbar}$  is

- (a)  $\sqrt{\frac{2}{L}} \left( \sin \frac{\pi x}{L} - \sin \frac{2\pi x}{L} \right) e^{-i\pi/6}$   
 (b)  $\sqrt{\frac{2}{L}} \left( \sin \frac{\pi x}{L} + \sin \frac{3\pi x}{L} \right) e^{-i\pi/6}$   
 (c)  $\sqrt{\frac{2}{L}} \left( \sin \frac{\pi x}{L} - \sin \frac{3\pi x}{L} \right) e^{-i\pi/8}$

(d)  $\sqrt{\frac{2}{L}} \left( \sin \frac{\pi x}{L} + \sin \frac{3\pi x}{L} \right) e^{ein/6}$

40. The pressure  $P$  of a system of  $N$  particles contained in a volume  $V$  at a temperature  $T$  is given by

$$P = nk_B T - \frac{1}{2} a n^2 + \frac{1}{6} b n^3$$

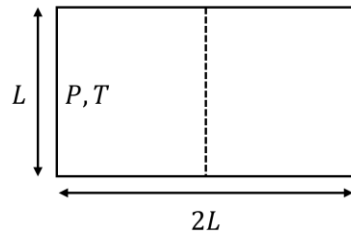
where  $n$  is the number density and  $a$  and  $b$  are temperature independent constants. If the system exhibits a gas-liquid transition, the critical temperature is

- (a)  $\frac{a}{bk_B}$  (b)  $\frac{a}{2b^2k_B}$   
(c)  $\frac{a^2}{2bk_B}$  (d)  $\frac{a^2}{b^2k_B}$

41. Consider a particle diffusing in a liquid contained in a large box. The diffusion constant of the particle in the liquid is  $1.0 \times 10^{-2} \text{ cm}^2/\text{s}$ . The minimum time after which the root-mean-squared displacement becomes more than 6 cm is

- (a) 10 min (b) 6 min  
(c) 30 min (d)  $\sqrt{6}$  min

42. A thermally insulated chamber of dimensions  $(L, L, 2L)$  is partitioned in the middle. One side of the chamber is filled with  $n$  moles of an ideal gas at a pressure  $P$  and temperature  $T$ , while the other side is empty. At  $t = 0$ , the partition is removed and the gas is allowed to expand freely. The time to reach equilibrium varies as



- (a)  $n^{1/3} L^{-1} T^{1/2}$  (b)  $n^{2/3} L T^{-1/2}$   
(c)  $n^0 L T^{-1/2}$  (d)  $n L^{-1} T^{1/2}$

43. The maximum intensity of solar radiation is at the wavelength of  $\lambda_{\text{sun}} \sim 5000 \text{ \AA}$  and corresponds to its surface temperature  $T_{\text{sun}} \sim 10^4 \text{ K}$ . If the wavelength of the

maximum intensity of an X-ray star is  $5 \text{ \AA}$ , its surface temperature is of the order of

- (a)  $10^{16} \text{ K}$  (b)  $10^{14} \text{ K}$   
(c)  $10^{10} \text{ K}$  (d)  $10^7 \text{ K}$

44. The full scale of a 3-bit digital-to-analog (DAC) converter is 7 V. Which of the following tables represents the output voltage of this 3-bit DAC for the given set of input bits?

(a)

Input bits	Output voltage
000	0
001	1
010	2
011	3

(c)

Input bits	Output voltage
000	1.25
001	2.5
010	3.75
011	5

(b)

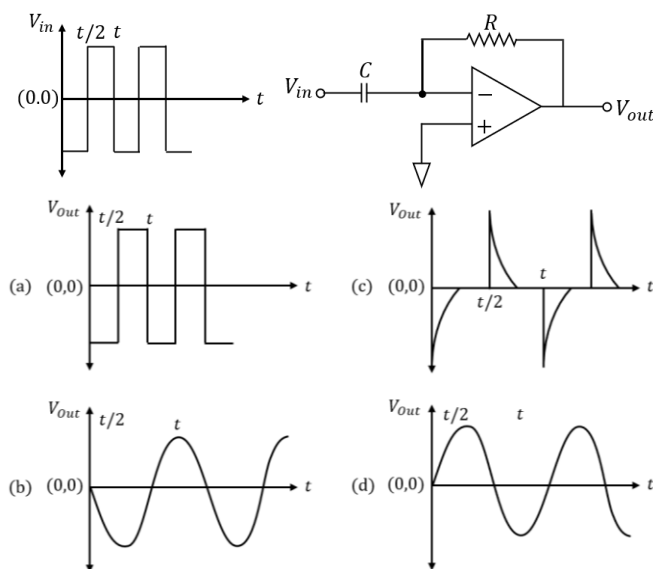
Input bits	Output voltage
000	0
001	1.25
010	2.5
011	3.75

(d)

Input bits	Output voltage
000	1
001	2
010	3



45. The input  $V_i$  to the following circuit is a square wave as shown in the following figure :  
Which of the waveforms  $V_o$  best describes the output?



46. Two signals  $A_1 \sin(\omega t)$  and  $A_2 \cos(\omega t)$  are fed into the input and the reference channels, respectively, of a lock-in amplifier. The amplitude of each signal is 1 V. The time constant of the lock-in amplifier is such that any signal of frequency larger than  $\omega$  is filtered out. The output of the lock-in amplifier is

- (a) 2 V (b) 1 V  
(c) 0.5 V (d) 0 V

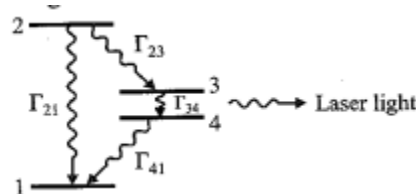
47. A photon energy 115.62 keV ionizes a K-shell electron of a Be atom. One L-shell electron jumps to the K-shell to fill this vacancy and emits a photon of energy 109.2 keV in the process. If the ionization potential for the L-shell is 6.4 keV, the kinetic energy of the ionized electron is  
(a) 6.42 keV (b) 12.82 keV  
(c) 20 eV (d) 320 V

48. The value of the Lande  $g$ -factor for a fine structure level defined by the quantum

numbers  $L = 1$  and  $J = 2$  and  $S = 1$ , is

- (a) 11/6 (b) 4/3  
(c) 8/3 (d) 3/2

49. The electronic energy level diagram of a molecule is shown in the following figure.



Let  $\Gamma_{ij}$  denote the decay rate for a transition from the level  $i$  and, . The molecules are optically pumped from level 1 to 2. For the transition from level 3 to level 4 to be a lasing transition, the decay rates have to satisfy

- (a)  $\Gamma_{21} > \Gamma_{23} > \Gamma_{41} > \Gamma_{34}$   
(b)  $\Gamma_{21} > \Gamma_{41} > \Gamma_{23} > \Gamma_{34}$   
(c)  $\Gamma_{41} > \Gamma_{23} > \Gamma_{21} > \Gamma_{34}$   
(d)  $\Gamma_{41} > \Gamma_{21} > \Gamma_{34} > \Gamma_{23}$

50. Sodium Chloride (NaCl) crystal is a face centred cubic lattice, with a basis consisting of  $\text{Na}^+$  and  $\text{Cl}^-$  ions separated by half the body diagonal of a unit cube. Which of the planes corresponding to the Miller indices given below will not give rise to Bragg reflection of X-rays ?

- (a) (2 2 0) (b) (2 4 2)  
(c) (2 2 1) (d) (3 1 1)

51. The dispersion relation for the electrons in the conduction band of a semiconductor is given by  $E = E_0 + \alpha k^2$ , where  $\alpha$  and  $E_0$  are constants. If  $\omega_c$  is the cyclotron resonance frequency of the conduction band electrons in a magnetic field  $B$ , the value of  $\alpha$  is

- (a)  $\frac{\hbar^2 \omega_c}{4eB}$  (b)  $\frac{2\hbar^2 \omega_c}{eB}$   
(c)  $\frac{\hbar^2 \omega_c}{eB}$  (d)  $\frac{\hbar^2 \omega_c}{2eB}$

52. Hard discs of radius  $R$  are arranged in a two-dimensional triangular lattice. What is the fractional area occupied by the discs in the closests possible packing ?

(a)  $\frac{\pi\sqrt{3}}{6}$

(b)  $\frac{\pi}{3\sqrt{2}}$

(c)  $\frac{\pi\sqrt{2}}{5}$

(d)  $\frac{2\pi}{7}$

53. Which of the following elementary particle processes does not conserve strangeness ?

(a)  $\pi^0 + p \rightarrow K^+ + \Lambda^0$

(b)  $\pi^- + p \rightarrow K^0 + \Lambda^0$

(c)  $\Delta^0 \rightarrow \pi^0 + n$

(d)  $K^0 \rightarrow \pi^+ + \pi^-$

54. A deuteron  $d$  captures a charged pion  $\pi^-$  in the  $l = 1$  state, and subsequently decays into a pair of neutrons ( $n$ ) via strong interaction.

Given that the intrinsic parities of  $\pi^-$ ,  $d$  and  $n$  are  $-1$ ,  $+1$  and  $+1$  respectively, the spin-wavefunction of the final state neutrons is a

(a) linear combination of a singlet and a triplet.

(b) singlet

(c) triplet

(d) doublet

55. The reaction  ${}^{63}\text{Cu}_{29} + p \rightarrow {}^{63}\text{Zn}_{30} + n$  is followed by a prompt  $\beta$ -decay of zinc

${}^{63}\text{Zn}_{30} \rightarrow {}^{63}\text{Cu}_{29} + e^+ + \nu_e$ . If the maximum energy of the positron is  $2.4\text{MeV}$ , the  $Q$ -value of the original reaction in  $\text{MeV}$  is nearest to

[Take the masses of electrons, proton and neutron to be  $0.5\text{MeV}/c^2$ ,  $938\text{MeV}/c^2$  and  $939.5\text{MeV}/c^2$ , respectively].

(a)  $-4.4$

(b)  $-2.4$

(c)  $-4.8$

(d)  $-3.4$

#### ❖ ANSWER KEY

21. a	22. c	23. b	24. c	25. a
26. a	27. c	28. b	29. c	30. d
31. c	32. b	33. b	34. c	35. c
36. c	37. c	38. a	39. a	40. c
41. d	42. d	43. c	44. c	45. d
46. c	47. b	48. b	49. b	50. b
51. c	52. b	53. b	54. b	55. c
56. c	57. a	58. c	59. d	60. c
61. a	62. c	63. d	64. a	65. b
66. d	67. c	68. d	69. c	70. c
71. d	72. a	73. d	74. b	75. a