



D PHYSICS

CSIR-NET, GATE, ALL SET, JEST, IIT-JAM, BARC

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❖ CSIR-UGC-NET/JRF- DEC - 2018 PHYSICAL SCIENCES BOOKLET - [A]

➤ PART-B

1. One of the eigenvalues of the matrix e^A is e^a ,

where $A = \begin{pmatrix} a & 0 & 0 \\ 0 & 0 & a \\ 0 & a & 0 \end{pmatrix}$. The product of the

other two eigenvalues of e^A is

- (a) e^{2a} (b) e^{-a}
(c) e^{-2a} (d) 1

2. The polynomial $f(x) = 1 + 5x + 3x^2$ is written as a linear combination of the Legendre polynomials

$$\left(P_0(x) = 1, P_1(x) = x, P_2(x) = \frac{1}{2}(3x^2 - 1) \right)$$

as $\sum_n c_n P_n(x)$. The value of c_0 is

- (a) $\frac{1}{4}$ (b) $\frac{1}{2}$
(c) 2 (d) 4

3. The value of the integral $\oint_C \frac{dz \tanh 2z}{z \sin \pi z}$, where C is a circle of radius $\frac{\pi}{2}$, traversed counter-clockwise, with centre at $z = 0$, is

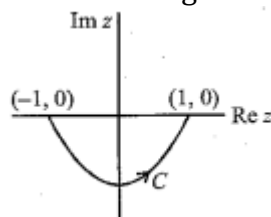
- (a) 4 (b) $4i$
(c) $2i$ (d) 0

4. A particle of mass m , moving along the x -direction, experiences a damping force $-\gamma v^2$, where γ is a constant and v is its instantaneous speed. If the speed at $t = 0$ is v_0 , the speed at time t is

(a) $v_0 e^{-\frac{\gamma v_0 t}{m}}$ (b) $\frac{v_0}{1 + \ln\left(1 + \frac{\gamma v_0 t}{m}\right)}$

(c) $\frac{m v_0}{m + \gamma v_0 t}$ (d) $\frac{2 v_0}{1 + e^{\frac{\gamma v_0 t}{m}}}$

5. The integral $I = \int_C e^z dz$ is evaluated from the point $(-1, 0)$ to $(1, 0)$ along the contour C , which is an arc of the parabola $y = x^2 - 1$, as shown in the figure.



The value of I is

- (a) 0 (b) $2 \sinh 1$
(c) $e^{2i} \sinh 1$ (d) $e + e^{-1}$

6. In terms of arbitrary constant A and B , the general solution to the differential equation

$$x^2 \frac{d^2 y}{dx^2} + 5x \frac{dy}{dx} + 3y = 0, \text{ is}$$

- (a) $y = \frac{A}{x} + Bx^3$ (b) $y = Ax + \frac{B}{x^3}$
(c) $y = Ax + Bx^3$ (d) $y = \frac{A}{x} + \frac{B}{x^3}$

7. In the attractive Kepler problem described by the central potential $V(r) = -\frac{k}{r}$, where k is a positive constant, a particle of mass m with a non-zero angular momentum can never reach the centre due to the centrifugal barrier. If we modify the potential to $V(r) = -\frac{k}{r} - \frac{\beta}{r^3}$ one finds that there is a critical value of the angular momentum ℓ_c below which there is no centrifugal barrier. This value of ℓ_c is

- (a) $[12 \text{ km}^2 \beta]^{1/2}$ (b) $[12 \text{ km}^2 \beta]^{-1/2}$
(c) $[12 \text{ km}^2 \beta]^{1/4}$ (d) $[12 \text{ km}^2 \beta]^{-1/4}$

8. The time period of a particle of mass m , undergoing small oscillations around $x = 0$,

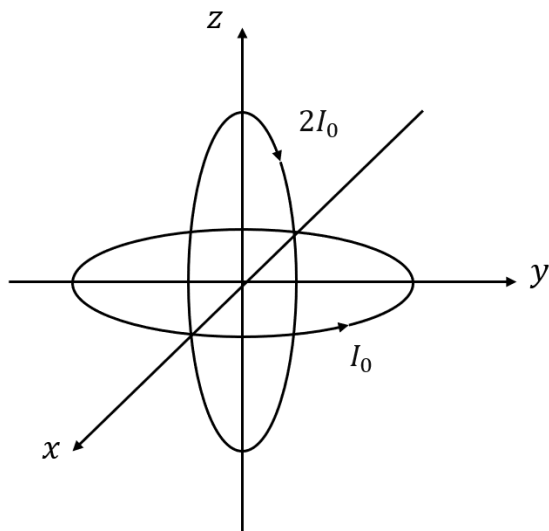
in the potential $V = V_0 \cosh\left(\frac{x}{L}\right)$, is

- (a) $\pi \sqrt{\frac{mL^2}{V_0}}$ (b) $2\pi \sqrt{\frac{mL^2}{2V_0}}$
(c) $2\pi \sqrt{\frac{mL^2}{V_0}}$ (d) $2\pi \sqrt{\frac{2mL^2}{V_0}}$

9. Consider the decay $A \rightarrow B + C$ of a relativistic spin $-\frac{1}{2}$ particle A . Which of the following statements is true in the rest frame of the particle A ?

- (a) The spin of both B and C may be $1/2$
(b) The sum of the masses of B and C is greater than the mass of A
(c) The energy of B is uniquely determined by the masses of the particles
(d) The spin of both B and C may be integral

10. Two current-carrying circular loops, each of radius R , are placed perpendicular to each other, as shown in the figure below.

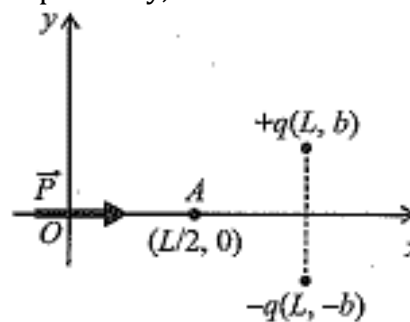


The loop in the xy -plane carries a current I_0 while that in the xz -plane carries a current $2I_0$. The resulting magnetic field $\vec{B}$ at the origin is

- (a) $\frac{\mu_0 I_0}{2R} [2\hat{j} + \hat{k}]$ (b) $\frac{\mu_0 I_0}{2R} [2\hat{j} - \hat{k}]$
(c) $\frac{\mu_0 I_0}{2R} [-2\hat{j} + \hat{k}]$ (d) $\frac{\mu_0 I_0}{2R} [-2\hat{j} - \hat{k}]$

11. An electric dipole of dipole moment $\vec{P} = qb\hat{i}$ is placed at the origin in the vicinity of two charges $+q$ and $-q$ at (L, b) and $(L, -b)$,

respectively, as shown in the figure below.



The electrostatic potential at the point $\left(\frac{L}{2}, 0\right)$ is

- (a) $\frac{qb}{\pi\epsilon_0} \left(\frac{1}{L^2} + \frac{2}{L^2 + 4b^2}\right)$ (b) $\frac{4qbl}{\pi\epsilon_0 [L^2 + 4b^2]^{3/2}}$
(c) $\frac{qb}{\pi\epsilon_0 L^2}$ (d) $\frac{3qb}{\pi\epsilon_0 L^2}$

12. A monochromatic and linearly polarized light is used in a Young's double slit experiment. A linear polarizer, whose pass axis is at an angle 45° to the polarization of the incident wave, is placed in front of one of the slits. If $I_{\max}$ and $I_{\min}$, respectively, denote the maximum and minimum intensities of the interference pattern on the screen, the visibility, defined as the ratio $\frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}}$, is

- (a) $\frac{\sqrt{2}}{3}$ (b) $\frac{2}{3}$
(c) $\frac{2\sqrt{2}}{3}$ (d) $\sqrt{\frac{2}{3}}$

13. An electromagnetic wave propagates in a nonmagnetic medium with relative permittivity $\epsilon = 4$. The magnetic field for this wave is

- $\vec{H}(x, y) = \hat{k} H_0 \cos(\omega t - \alpha x - \alpha\sqrt{3}y)$,
where H_0 is a constant. The corresponding electric field $\vec{E}(x, y)$ is
(a) $\frac{1}{4} \mu_0 H_0 c (-\sqrt{3}\hat{i} + \hat{j}) \cos(\omega t - \alpha x - \alpha\sqrt{3}y)$
(b) $\frac{1}{4} \mu_0 H_0 c (\sqrt{3}\hat{i} + \hat{j}) \cos(\omega t - \alpha x - \alpha\sqrt{3}y)$
(c) $\frac{1}{4} \mu_0 H_0 c (\sqrt{3}\hat{i} - \hat{j}) \cos(\omega t - \alpha x - \alpha\sqrt{3}y)$
(d) $\frac{1}{4} \mu_0 H_0 c (-\sqrt{3}\hat{i} - \hat{j}) \cos(\omega t - \alpha x - \alpha\sqrt{3}y)$

14. The ground state energy of an anisotropic harmonic oscillator described by the potential $V(x, y, z) = \frac{1}{2} m \omega^2 x^2 + 2m \omega^2 y^2 + 8m \omega^2 z^2$ (in units of $\hbar\omega$) is
(a) $5/2$ (b) $7/2$

(c) $3/2$ (d) $1/2$

15. The product $\Delta x \Delta p$ of uncertainties in the position and momentum of a simple harmonic oscillator of mass m and angular frequency ω in the ground state $|0\rangle$, is $\hbar/2$. The value of the product $\Delta x \Delta p$ in the state $e^{-i\hat{p}l/\hbar}|0\rangle$, where l is a constant and $\hat{p}$ is the momentum operator) is

(a) $\frac{\hbar}{2} \sqrt{\frac{m\omega l^2}{\hbar}}$

(b) $\hbar$

(c) $\frac{\hbar}{2}$

(d) $\frac{\hbar^2}{m\omega l^2}$

16. Let the wavefunction of the electron in a hydrogen atom be

$$\psi(\vec{r}) = \frac{1}{\sqrt{6}} \phi_{200}(\vec{r}) + \sqrt{\frac{2}{3}} \phi_{21-1}(\vec{r}) - \frac{1}{\sqrt{6}} \phi_{100}(\vec{r})$$

where $\phi_{nlm}(\vec{r})$ are the eigenstates of the Hamiltonian in the standard notation. The expectation value of the energy in this state is

(a) -10.8eV

(b) -6.2eV

(c) -9.5eV

(d) -5.1eV

17. Three identical spin $-\frac{1}{2}$ particles of mass m are confined to a one-dimensional box of length L , but are otherwise free. Assuming that they are non-interacting, the energies of the lowest two energy eigenstates, in units of $\frac{\pi^2 \hbar^2}{2mL^2}$, are

(a) 3 and 6

(b) 6 and 9

(c) 6 and 11

(d) 3 and 9

18. The heat capacity C_V at constant volume of a metal, as a function of temperature, is $\alpha T + \beta T^3$, where α and β are constants. The temperature dependence of the entropy at constant volume is

(a) $\alpha T + \frac{1}{3} \beta T^3$

(b) $\alpha T + \beta T^3$

(c) $\frac{1}{2} \alpha T + \frac{1}{3} \beta T^3$

(d) $\frac{1}{2} \alpha T + \frac{1}{4} \beta T^3$

19. The rotational energy levels of a molecule are $E_l = \frac{\hbar^2}{2I_0} l(l+1)$, where $l = 0, 1, 2, \dots$ and I_0 is its mo. ment of inertia. The contribution of the rotational motion to the Helmholtz free energy per molecule at low temperature in a

dilute gas of these molecules, is approximately

(a) $-k_B T \left(1 + \frac{\hbar^2}{I_0 k_B T}\right)$

(b) $-k_B T e^{-\frac{\hbar^2}{I_0 k_B T}}$

(c) $-k_B T$

(d) $-3k_B T e^{-\frac{\hbar^2}{I_0 k_B T}}$

20. The vibrational motion of a diatomic molecule may be considered to be that of a simple harmonic oscillator with angular frequency ω . If a gas of these molecules is at a temperature T , what is the probability that a randomly picked molecule will be found in its lowest vibrational state?

(a) $1 - e^{-\frac{\hbar\omega}{k_B T}}$

(b) $e^{-\frac{\hbar\omega}{2k_B T}}$

(c) $\tanh\left(\frac{\hbar\omega}{k_B T}\right)$

(d) $\frac{1}{2} \text{cosech}\left(\frac{\hbar\omega}{2k_B T}\right)$

21. Consider an ideal Fermi gas in a grand canonical ensemble at a constant chemical potential. The variance of the occupation number of the single particle energy level with mean occupation number $\bar{n}$ is

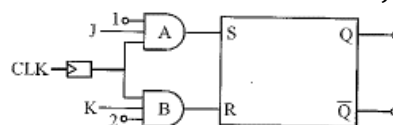
(a) $\bar{n}(1 - \bar{n})$

(b) $\sqrt{\bar{n}}$

(c) $\bar{n}$

(d) $1/\sqrt{\bar{n}}$

22. Consider the following circuit, consisting of an RS flip-flop and two AND gates. Which of the following connections will allow the entire circuit to act as a JK flip-flop?



(a) connect Q to pin 1 and $\bar{Q}$ to pin 2

(b) connect Q to pin 2 and $\bar{Q}$ to pin 1

(c) connect Q to K input and $\bar{Q}$ to J input

(d) connect Q to J input and $\bar{Q}$ to K input

23. The truth table below gives the value $Y(A, B, C)$, where A, B and C are binary variables.

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1

1	0	1	0
1	1	0	0
1	1	1	1

The output Y can be represented by

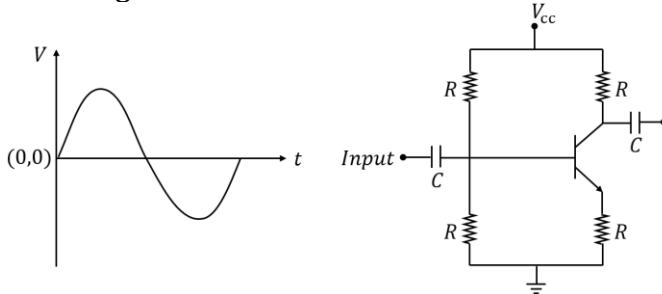
(a) $Y = \overline{A}BC + \overline{A}B\overline{C} + \overline{A}BC + AB\overline{C}$

(b) $Y = \overline{A}\overline{B}\overline{C} + \overline{A}BC + A\overline{B}\overline{C} + ABC$

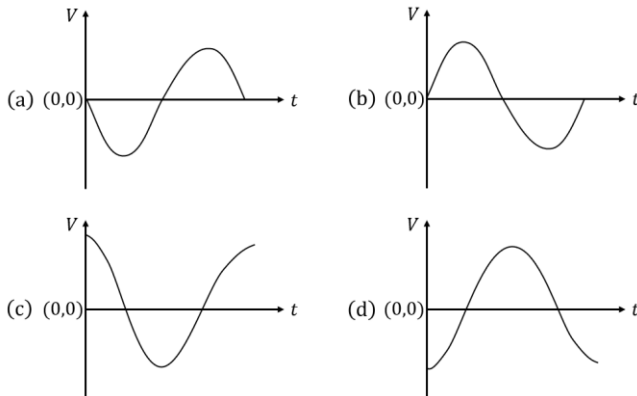
(c) $Y = \overline{A}\overline{B}C + \overline{A}BC + A\overline{B}C + ABC$

(d) $Y = \overline{A}\overline{B}\overline{C} + \overline{A}B\overline{C} + A\overline{B}\overline{C} + ABC$

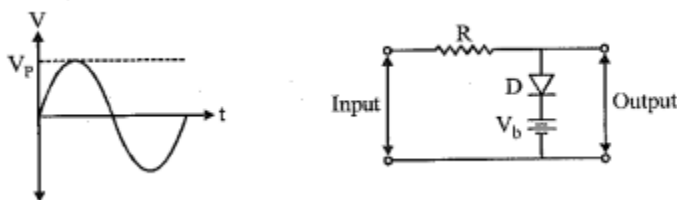
24. A sinusoidal signal is an input to the following circuit :



Which of the following graphs best describes the output waveform?

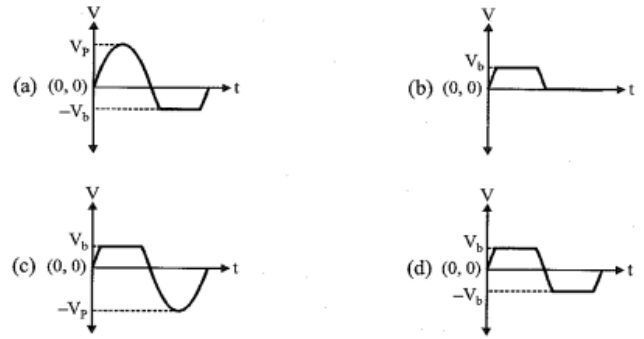


25. A sinusoidal voltage having a peak value of V_p is an input to the following circuit, in which the DC voltage is V_b .



Assuming an ideal diode, which of the following best describes the output

waveform?



➤ PART - C

26. The Green's function $G(x, x')$ for the equation

$$\frac{d^2 y(x)}{dx^2} = f(x), \text{ with the boundary values}$$

$y(0) = 0$ and $y(1) = 0$, is

(a) $G(x, x') = \begin{cases} \frac{1}{2}x(1-x'), & 0 < x < x' < 1 \\ \frac{1}{2}x'(1-x), & 0 < x' < x < 1 \end{cases}$

(b) $G(x, x') = \begin{cases} x(x'-1), & 0 < x < x' < 1 \\ x'(1-x), & 0 < x' < x < 1 \end{cases}$

(c) $G(x, x') = \begin{cases} -\frac{1}{2}x(1-x), & 0 < x < x' < 1 \\ \frac{1}{2}x'(1-x), & 0 < x' < x < 1 \end{cases}$

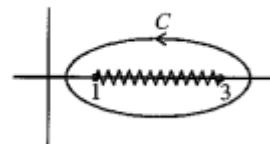
(d) $G(x, x') = \begin{cases} x(x'-1), & 0 < x < x' < 1 \\ x'(x-1), & 0 < x' < x < 1 \end{cases}$

27. A 4×4 complex matrix A satisfies the relation $A^\dagger A = 4I$, where I is the 4×4 identity matrix. The number of independent real parameters of A is

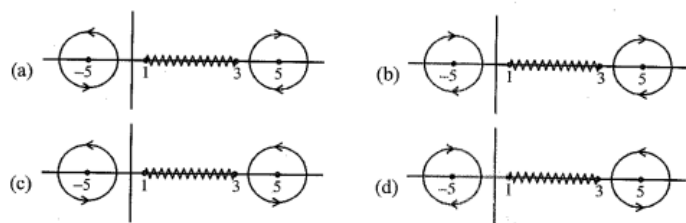
- (a) 32 (b) 10
(c) 12 (d) 16

28. The contour C of the following integral

$$\oint_C dz \frac{\sqrt{(z-1)(z-3)}}{(z^2-25)^3}, \text{ in the complex } z\text{-plane is shown in the figure below.}$$



This integral is equivalent to an integral along the contours



29. The value of the integral $\int_0^1 x^2 dx$, evaluated using the trapezoidal rule with a step size of 0.2, is

- (a) 0.30 (b) 0.39
(c) 0.34 (d) 0.27

30. The motion of a particle in one-dimension is described by the Lagrangian

$$L = \frac{1}{2} \left(\left(\frac{dx}{dt} \right)^2 - x^2 \right)$$

in suitable units. The value of the action along the classical path from $x = 0$ at $t = 0$ to $x = x_0$ at $t = t_0$, is

- (a) $\frac{x_0^2}{2\sin^2 t_0}$ (b) $\frac{1}{2}x_0^2 \tan t_0$
(c) $\frac{1}{2}x_0^2 \cot t_0$ (d) $\frac{x_0^2}{2\cos^2 t_0}$

31. The Hamiltonian of a classical one-dimensional harmonic oscillator is $H = \frac{1}{2}(p^2 + x^2)$, in suitable units. The total time derivative of the dynamical variable $(p + \sqrt{2}x)$ is

- (a) $\sqrt{2}p - x$ (b) $p - \sqrt{2}x$
(c) $p + \sqrt{2}x$ (d) $x + \sqrt{2}p$

32. A relativistic particle of mass m and charge e is moving in a uniform electric field of strength b . Starting from rest at $t = 0$, how much time will it take to reach the speed $c/2$?

- (a) $\frac{1}{\sqrt{3}} \frac{mc}{e\epsilon}$ (b) $\frac{mc}{e\epsilon}$
(c) $\sqrt{2} \frac{mc}{e\epsilon}$ (d) $\sqrt{\frac{3}{2}} \frac{mc}{e\epsilon}$

33. In an inertial frame, uniform electric and magnetic fields $\vec{E}$ and $\vec{B}$ are perpendicular to each other and satisfy $|\vec{E}|^2 - |\vec{B}|^2 = 29$ (in suitable units). In another inertial frame, which moves at a constant velocity with respect to the first frame, the magnetic field is $2\sqrt{5}\hat{k}$. In the second frame, an electric field

consistent with the previous observations is

- (a) $\frac{7}{\sqrt{2}}(\hat{i} + \hat{j})$ (b) $7(\hat{i} + \hat{k})$
(c) $\frac{7}{\sqrt{2}}(\hat{i} + \hat{k})$ (d) $7(\hat{i} + \hat{j})$

34. Electromagnetic wave of angular frequency ω is propagating in a medium in which, over a band of frequencies, the refractive index is $n(\omega) \approx 1 - \left(\frac{\omega}{\omega_0} \right)^2$, where ω_0 is a constant.

The ratio $\frac{v_g}{v_p}$ of the group velocity to the phase velocity at $\omega = \frac{\omega_0}{2}$ is

- (a) 3 (b) 1/4
(c) 2/3 (d) 2

35. A rotating spherical shell of uniform surface charge and mass density has total mass M and charge Q . If its angular momentum is L and magnetic moment is μ , then the ratio μ/L is

- (a) $Q/3M$ (b) $2Q/3M$
(c) $Q/2M$ (d) $3Q/4M$

36. Consider the operator $A_x = L_y p_z - L_z p_y$, where L_i and p_i denote, respectively, the components of the angular momentum and momentum operators. The commutator $[A_x, x]$, where x is the x -component of the position operator, is

- (a) $-i\hbar(zp_z + yp_y)$ (b) $-i\hbar(zp_z - yp_y)$
(c) $i\hbar(zp_z + yp_y)$ (d) $i\hbar(zp_z - yp_y)$

37. A one-dimensional system is described by the Hamiltonian $H = \frac{p^2}{2m} + \lambda|x|$, where $\lambda > 0$. The ground state energy varies as a function of λ as

- (a) $\lambda^{5/3}$ (b) $\lambda^{2/3}$
(c) $\lambda^{4/3}$ (d) $\lambda^{1/3}$

38. If the position of the electron in the ground state of a hydrogen atom is measured, the probability that it will be found at a distance $r \geq a_0$ (a_0 being Bohr radius) is nearest to

- (a) 0.91 (b) 0.66
(c) 0.32 (d) 0.13

39. A system of spin- $\frac{1}{2}$ particles is prepared to be in the eigenstate of σ_z with eigenvalue $+1$.

The system is rotated by an angle of 60° about the x -axis. After the rotation, the fraction of the particles that will be measured to be in the eigenstate of σ_z with eigenvalue $+1$ is

- (a) $1/3$ (b) $2/3$
(c) $1/4$ (d) $3/4$

40. The Hamiltonian of a one-dimensional Ising model of N spins (N large) is

$$H = -J \sum_{i=1}^N \sigma_i \sigma_{i+1}$$

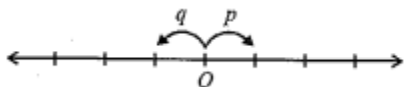
where the spin $\sigma_i = \pm 1$ and J is a positive constant. At inverse temperature $\beta = \frac{1}{k_B T}$, the correlation function between the nearest neighbour spins $\langle \sigma_i \sigma_{i+1} \rangle$ is

- (a) $\frac{e^{-\beta J}}{(e^{\beta J} + e^{-\beta J})}$ (b) $e^{-2\beta J}$
(c) $\tanh(\beta J)$ (d) $\coth(\beta J)$

41. At low temperatures, in the Debye approximation, the contribution of the phonons to the heat capacity of a two-dimensional solid is proportional to

- (a) T^2 (b) T^3
(c) $T^{1/2}$ (d) $T^{3/2}$

42. A particle hops on a one-dimensional lattice with lattice spacing a . The probability of the particle to hop to the neighbouring site to its right is p , while the corresponding probability to hop to the left is $q = 1 - p$. The root-mean-squared deviation $\Delta x = \sqrt{\langle x^2 \rangle - \langle x \rangle^2}$ in displacement after N steps, is

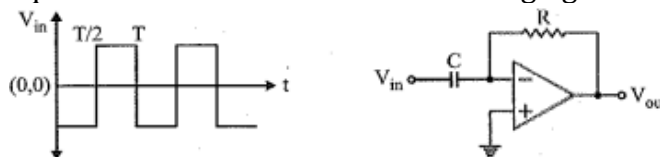


- (a) $a\sqrt{Npq}$ (b) $aN\sqrt{pq}$
(c) $2a\sqrt{Npq}$ (d) $a\sqrt{N}$

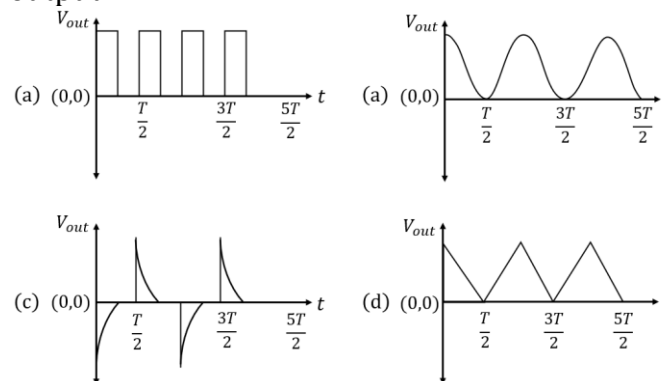
43. The energy levels accessible to a molecule have energies $E_1 = 0$, $E_2 = \Delta$ and $E_3 = 2\Delta$ (where Δ is a constant). A gas of these molecules is in thermal equilibrium at temperature T . The specific heat at constant volume in the high temperature limit ($k_B T \gg \Delta$) varies with temperature as

- (a) $1/T^{3/2}$ (b) $1/T^3$
(c) $1/T$ (d) $1/T^2$

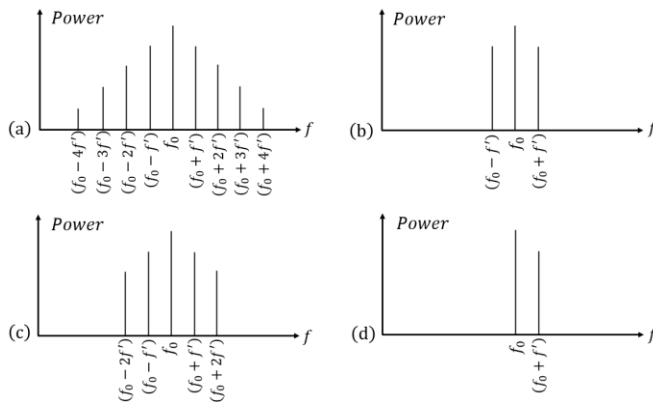
44. The input V_i to the following circuit is a square wave as shown in the following figure.



Which of the waveforms best describes the output?



45. The amplitude of a carrier signal of frequency f_0 is sinusoidally modulated at a frequency $f' \neq f_0$. Which of the following graphs best describes its power spectrum?



46. The standard deviation of the following set of data : {10.0, 10.0, 9.9, 9.9, 9.8, 9.9, 9.9, 9.9, 9.8, 9.9}

- (a) 0.10 (b) 0.07
(c) 0.01 (d) 0.04

47. The diatomic molecule HF has an absorption line in the rotational band at 40 cm^{-1} for the isotope ^{18}F . The corresponding line for the isotope ^{19}F will be shifted by approximately

- (a) 0.05 cm^{-1} (b) 0.11 cm^{-1}
(c) 0.33 cm^{-1} (d) 0.01 cm^{-1}

48. The excited state ($n = 4, l = 2$) of an electron in an atom may decay to one or more of the lower energy levels shown in the diagram below.

$$n = 4 \rightarrow \prod_{l=0}^{l=1} l = 2$$

$$n = 3 \rightarrow$$

$$n = 2 \rightarrow$$

Of the total emitted light, a fraction $1/4$ comes from the decay to the state ($n = 2, l = 1$). Based on selection rules, the fractional intensity of the emission line due to the decay to the state ($n = 3, l = 1$) will be

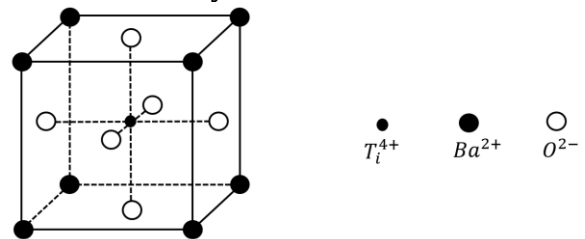
- (a) $3/4$ (b) $1/2$
(c) $1/4$ (d) 0

49. The volume of an optical cavity is 1 cm^3 . The number of modes it can support within a bandwidth of 0.1 nm , centred at $\lambda = 500 \text{ nm}$, is of the order of

- (a) 10^3 (b) 10^5
(c) 10^{10} (d) 10^7

50. Barium Titanate (BaTiO_3) crystal has a cubic perovskite structure, where the Ba^{2+} ions are

at the vertices of a unit cube, the O^{2-} ions are at the centres of the faces while the Ti^{4+} is at the centre. The number of optical phonon modes of the crystal is



- (a) 12 (b) 15
(c) 5 (d) 18

51. The dispersion relation of optical phonons in a cubic crystal is given by $\omega(k) = \omega_0 - ak^2$, where ω_0 and a are positive constants. The contribution to the density of states due to these phonons with frequencies just below ω_0 is proportional to

- (a) $(\omega_0 - \omega)^{1/2}$ (b) $(\omega_0 - \omega)^{3/2}$
(c) $(\omega_0 - \omega)^2$ (d) $(\omega_0 - \omega)$

52. A silicon crystal is doped with phosphorus atoms. (The binding energy of a H atom is 13.6 eV , the dielectric constant of silicon is 12 and the effective mass of electron in the crystal is $0.4m_e$). The gap between the donor energy level and the bottom of the conduction band is nearest to

- (a) 0.01 eV (b) 0.08 eV
(c) 0.02 eV (d) 0.04 eV

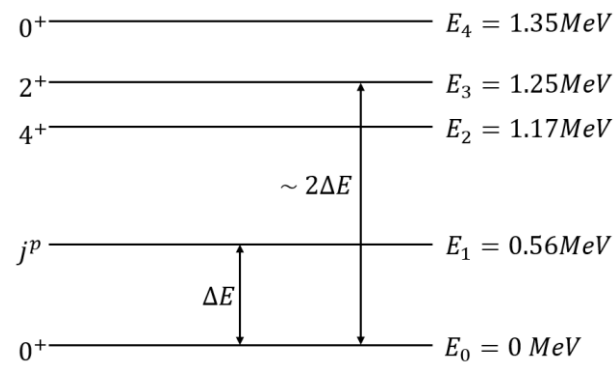
53. Assume that pion-nucleon scattering at low energies, in which isospin is conserved, is described by the effective interaction potential $V_{\text{eff}} = F(r) \vec{I}_x \cdot \vec{I}_N$, where $F(r)$ is a function of the radial separation r and $\vec{I}_m$ and $\vec{I}_N$ denote, respectively, the isospin vectors of a pion and the nucleon. The ratio $\sigma_{I=3/2} / \sigma_{I=1/2}$ of the scattering cross-sections corresponding to total isospins $I = 3/2$ and $1/2$, is

- (a) $3/2$ (b) $1/4$
(c) $5/4$ (d) $1/2$

54. A nucleus decays by the emission of a gamma ray from an excited state of spin-parity 2^+ to the ground state with spin-parity 0^+ . What is the type of the corresponding radiation?

- (a) magnetic dipole
- (b) electric quadrupole
- (c) electric dipole
- (d) magnetic quadrupole

55. The low lying energy levels due to the vibrational excitations of an even-even nucleus are shown in the figure below.



The spin-parity j^p of the level E_1 is

- (a) 1^+
- (b) 1^-
- (c) 2^-
- (d) 2^+

❖ ANSWER KEY

1. d	2. c	3.	4. c	5. b
6.	7. c	8. c	9. c	10. c
11. c	12. b	13. a	14. b	15. c
16. d	17. b	18. a	19. d	20. a
21. a	22. b	23. b	24. a	25. c
26. d	27. d	28. b	29. c	30. c
31. a	32. a	33. a	34. a	35. c
36. a	37. b	38. b	39. d	40. c
41. a	42. c	43. d	44. c	45. b
46. b	47. b	48. a	49. c	50. a
51. a	52. d	53. b	54. b	55. d