



D PHYSICS

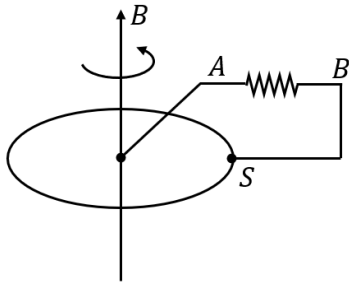
CSIR-NET,GATE , ALL SET, JEST, IIT-JAM, BARC

Contact: 8830156303 | 7741947669

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PART-B

1. A horizontal metal disc rotates about the vertical axis in a uniform magnetic field pointing up as shown in the figure. A circuit is made by connecting one end A of a resistor to the centre of the disc and the other end B to its edge through a sliding contact S. The current that flows through the resistor is



- (a) zero
(b) DC from A to B
(c) DC from B to A
(d) AC
2. A spin $-\frac{1}{2}$ particle is in the state $\chi = \frac{1}{\sqrt{11}} \begin{pmatrix} 1+i \\ 3 \end{pmatrix}$ in the eigenbasis of S^2 and S_x . If we measure S_z the probabilities of getting $+\frac{\hbar}{2}$ and $-\frac{\hbar}{2}$, respectively, are
- (a) $\frac{1}{2}$ and $\frac{1}{2}$
(b) $\frac{2}{11}$ and $\frac{9}{11}$
(c) 0 and 1
(d) $\frac{1}{11}$ and $\frac{3}{11}$
3. Which of the following functions cannot be the real part of a complex analytic function of $z = x + iy$?
- (a) x^2y
(b) $x^2 - y^2$
(c) $x^3 - 3xy^2$
(d) $3x^2y - y - y^3$
4. The motion of a particle of mass m in one dimension is described by the Hamiltonian

$H = \frac{p^2}{2m} + \frac{1}{2}m\omega^2x^2 + \lambda x$. What is the difference between the (quantized) energies of the first two levels? (In the following, $\langle x \rangle$ is the expectation value of x in the ground state)

- (a) $\hbar\omega - \lambda\langle x \rangle$
(b) $\hbar\omega + \lambda\langle x \rangle$
(c) $\hbar\omega + \frac{\lambda^2}{2m\omega^2}$
(d) $\hbar\omega$

5. Let ψ_{mim} denote the eigenfunctions of a Hamiltonian for a spherically symmetric potential $V(r)$. The expectation value of L_z in the state $\psi = \frac{1}{6}[\psi_{200} + \sqrt{5}\psi_{210} + \sqrt{10}\psi_{21-1} + \sqrt{20}\psi_{211}]$ is

- (a) $-\frac{5}{18}\hbar$
(b) $\frac{5}{6}\hbar$
(c) \hbar
(d) $\frac{5}{18}\hbar$

6. Three identical spin $-\frac{1}{2}$ fermions are to be distributed in two non-degenerate distinct energy levels. The number of ways this can be done is

- (a) 8
(b) 4
(c) 3
(d) 2

7. Let A, B and C be functions of phase space variables (coordinates and momenta of a mechanical system). If

$\{A, B\}$ represents the Poisson bracket, the value of $\{A, \{B, C\}\}$ is given by

- (a) 0
(b) $\{B, \{C, A\}\}$
(c) $\{A, \{C, B\}\}$
(d) $\{\{C, A\}, B\}$

8. If A, B and C are non-zero Hermitian operators, which of the following relations must be false?

(a) $[A, B] = C$ (b) $AB + BA = C$
(c) $ABA = C$ (d) $A + B = C$

9. The expression

$$\left(\frac{\partial^2}{\partial x_1^2} + \frac{\partial^2}{\partial x_2^2} + \frac{\partial^2}{\partial x_3^2} + \frac{\partial^2}{\partial x_4^2} \right) \frac{1}{(x_1^2 + x_2^2 + x_3^2 + x_4^2)}$$

is proportional to

(a) $\delta(x_1 + x_2 + x_3 + x_4)$
(b) $\delta(x_1)\delta(x_2)\delta(x_3)\delta(x_4)$
(c) $(x_1^2 + x_2^2 + x_3^2 + x_4^2)^{-3/2}$
(d) $(x_1^2 + x_2^2 + x_3^2 + x_4^2)^{-2}$

10. Given that the integral $\int_0^\infty \frac{dx}{y^2 + x^2} = \frac{\pi}{2y}$, the

value of $\int_0^\infty \frac{dx}{(y^2 + x^2)^2}$ is

(a) $\frac{\pi}{y^3}$ (b) $\frac{\pi}{4y^3}$
(c) $\frac{\pi}{8y^3}$ (d) $\frac{\pi}{2y^3}$

11. The force between two long and parallel wires carrying currents I_1 and I_2 and separated by a distance D is proportional to

(a) $I_1 I_2 / D$ (b) $(I_1 + I_2) / D$
(c) $(I_1 I_2 / D)^2$ (d) $I_1 I_2 / D^2$

12. A loaded dice has the probabilities

$\frac{1}{21}, \frac{2}{21}, \frac{3}{21}, \frac{4}{21}, \frac{5}{21}$ and $\frac{6}{21}$ of turning up 1, 2, 3, 4, 5 and 6, respectively. If it is thrown twice, what is the probability that the sum of the numbers that turn up is even?

(a) $\frac{144}{441}$ (b) $\frac{225}{441}$
(c) $\frac{221}{441}$ (d) $\frac{220}{441}$

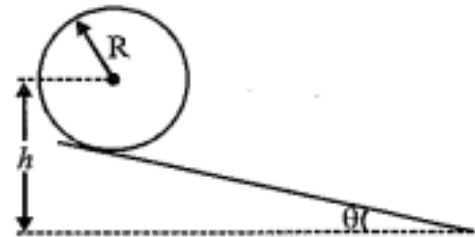
13. A particle moves in a potential $V = x^2 + y^2 + \frac{z^2}{2}$. Which component (s) of the angular momentum is / are constant (s) of motion?

(a) none
(b) L_x, L_y and L_z
(c) only L_x and L_y (d) only L_z

14. The Hamiltonian of a relativistic particle of rest mass m and momentum p is given by $H = \sqrt{p^2 + m^2} + V(x)$, in units in which the speed of light $c = 1$. The corresponding Lagrangian is

(a) $L = m\sqrt{1 + \dot{x}^2} - V(x)$
(b) $L = -m\sqrt{1 - \dot{x}^2} - V(x)$
(c) $L = \sqrt{1 + m\dot{x}^2} - V(x)$
(d) $L = \frac{1}{2}m\dot{x}^2 - V(x)$

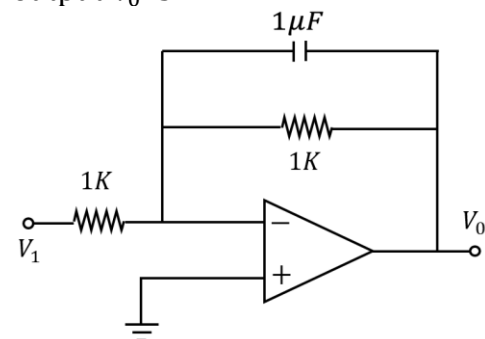
15. A ring of mass m and radius R rolls (without slipping) down an inclined plane starting from rest. If the centre of the ring is initially at a height h , the angular velocity when the ring reaches the base is



(a) $\sqrt{g/(h - R)} \tan \theta$
(b) $\sqrt{g/(h - R)}$
(c) $\sqrt{g(h - R)/R^2}$
(d) $\sqrt{2g/(h - R)}$

16. Consider the op-amp circuit shown in the figure.

If the input is a sinusoidal wave $V_i = 5\sin(1000t)$, then the amplitude of the output V_o is



(a) $\frac{5}{2}$ (b) 5
(c) $\frac{5\sqrt{2}}{2}$ (d) $5\sqrt{2}$

17. If one of the inputs of a J-K flip flop is high and the other is low, then the outputs Q and \bar{Q}
- oscillate between low and high in race-around condition
 - toggle and the circuit acts like a T flip flop
 - are opposite to the inputs
 - follow the inputs and the circuit acts like an R-S flip flop

18. Two monochromatic sources, L_1 , and L_2 , emit light at 600 and 700 nm, respectively. If their frequency bandwidths are 10^{-1} and 10^{-3} GHz, respectively, then the ratio of linewidth of L_1 and L_2 is approximately
- 100:1
 - 1:85
 - 75:1
 - 1:75

19. Let (V, A) and (V', A') denote two sets of scalar and vector potentials, and ψ a scalar function. Which of the following transformations leave the electric and magnetic fields (and hence Maxwell's equations) unchanged?

- $A' = A + \nabla\psi$ and $V = V - \frac{\partial\psi}{\partial t}$
- $A' = A - \nabla\psi$ and $V' = V + 2\frac{\partial\psi}{\partial t}$
- $A' = A + \nabla\psi$ and $V' = V + \frac{\partial\psi}{\partial t}$
- $A' = A - 2\nabla\psi$ and $V' = V - \frac{\partial\psi}{\partial t}$

20. Consider the melting transition of ice into water at constant pressure. Which of the following thermodynamic quantities does not exhibit a discontinuous change across the phase transition?
- internal energy
 - Helmholtz free energy
 - Gibbs free energy
 - entropy

21. Two different thermodynamic systems are described by the following equations of state:

$$\frac{1}{T^{(1)}} = \frac{3RN^{(1)}}{2U^{(1)}} \text{ and } \frac{1}{T^{(2)}} = \frac{5RN^{(2)}}{2U^{(2)}} \text{ where } T^{(1,2)}, N^{(1,2)} \text{ and } U^{(1,2)} \text{ are respectively, the}$$

temperatures; the mole numbers and the internal energies of the two systems, and R is the gas constant. Let U_{sat} denote the total energy when these two systems are put in contact and attain thermal equilibrium. The

ratio $\frac{U^{(1)}}{U_{\text{tot}}}$ is

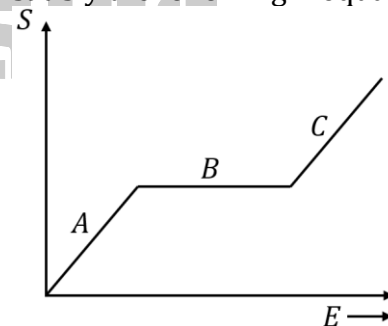
- $\frac{5N^{(2)}}{3N^{(1)}+5N^{(2)}}$
- $\frac{3N^{(1)}}{3N^{(1)}+5N^{(2)}}$
- $\frac{N^{(1)}}{N^{(1)}+N^{(2)}}$
- $\frac{N^{(2)}}{N^{(1)}+N^{(2)}}$

22. The speed v of the molecules of mass m of an ideal gas obeys Maxwell's velocity distribution law at an equilibrium temperature T . Let (v_x, v_y, v_z) denote the components of the velocity and k_B the Boltzmann constant. The average value of $(\alpha v_x - \beta v_y)^2$, where α and β are constants, is

- $(\alpha^2 - \beta^2)k_B T/m$
- $(\alpha^2 + \beta^2)k_B T/m$
- $(\alpha + \beta)^2 \cdot k_B T/m$
- $(\alpha - \beta)^2 k_B T/m$

23. The entropy S of a thermodynamic system as a function of energy E is given by the following graph

The temperatures of the phases A, B and C , denoted by T_A, T_B and T_C , respectively, satisfy the following inequalities:

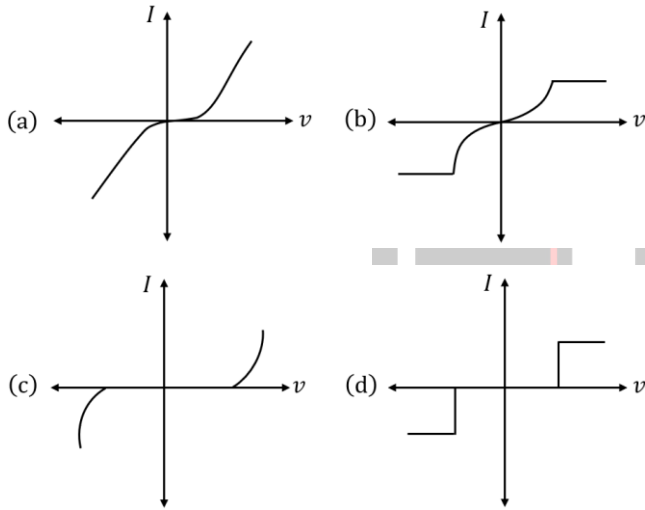


- $T_C > T_B > T_A$
- $T_A > T_C > T_B$
- $T_B > T_C > T_A$
- $T_B > T_A > T_C$

24. The physical phenomenon that cannot be used for memory storage applications is

- (a) large variation in magnetoresistance as a function of applied magnetic field
- (b) variation in magnetization of a ferromagnet as a function of applied magnetic field
- (c) variation in polarization of a ferroelectric as a function of applied electric field
- (d) variation in resistance of a metal as a function of applied electric field

25. Two identical Zener diodes are placed back to back in series and are connected to a variable DC power supply. The best representation of the I-V characteristics of the circuit is



❖ Part-C

26. A pendulum consists of a ring of mass M and radius R suspended by a massless rigid rod of length l attached to its rim. When the pendulum oscillates in the plane of the ring, the time period of oscillation is

- (a) $2\pi \sqrt{\frac{l+R}{g}}$
- (b) $\frac{2\pi}{\sqrt{g}} (l^2 + R^2)^{1/4}$
- (c) $2\pi \sqrt{\frac{2R^2 + 2Rl + l^2}{g(R+l)}}$
- (d) $\frac{2\pi}{\sqrt{g}} (2R^2 + 2Rl + l^2)^{1/4}$

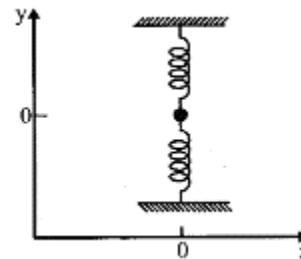
27. Spherical particles of a given material of density p are released from rest inside a liquid medium of lower density. The viscous drag force may be approximated by the Stoke's law, i.e, $F_l = 6\pi\eta Rv$, where η is the viscosity of the medium, R the radius of a particle and v its instantaneous velocity. If $\tau(m)$ is the time taken by a particle of mass m to reach half its terminal velocity, then the ratio $\tau(8m)/\tau(m)$ is

- (a) 8
- (b) 1/8
- (c) 4
- (d) 1/4

28. A system of N classical non-interacting particles, each of mass m , is at temperature T and is confined by the external potential $V(r) = \frac{1}{2}Ar^2$ (where A is a constant) in three dimensions. The internal energy of the system is

- (a) $3Nk_B T$
- (b) $\frac{3}{2}Nk_B T$
- (c) $N(2mA)^{3/2}k_B T$
- (d) $N \sqrt{\frac{A}{m}} \ln \left(\frac{k_B T}{m} \right)$

29. Consider a particle of mass m attached to two identical springs each of length l and spring constant k (see the figure below). The equilibrium configuration is the one where the springs are unstretched. There are no other external forces on the system. If the particle is given a small displacement along the x -axis, which of the following describes the equation of motion for small oscillations?



- (a) $m\ddot{x} + \frac{kx^3}{l^2} = 0$
- (b) $m\ddot{x} + kx = 0$
- (c) $m\ddot{x} + 2kx = 0$
- (d) $m\ddot{x} + \frac{kx^2}{l} = 0$

30. If $\psi(x) = A \exp(-x^4)$ is the eigenfunction of a one dimensional Hamiltonian with eigenvalue $E = 0$, the potential $V(x)$ (in units where $\hbar = 2m = 1$) is

- (a) $12x^2$ (b) $16x^6$
(c) $16x^6 + 12x^2$ (d) $16x^6 - 12x^2$

31. The electric field of an electromagnetic wave is given by $\vec{E} = E_0 \cos [\pi(0.3x + 0.4y - 1000t)]\hat{k}$. The associated magnetic field \vec{B} is

- (a) $10^{-3}E_0 \cos [\pi(0.3x + 0.4y - 1000t)]\hat{k}$
(b) $10^{-4}E_0 \cos [\pi(0.3x + 0.4y - 1000t)](4\hat{i} - 3\hat{j})$
(c) $E_0 \cos [\pi(0.3x + 0.4y - 1000t)](0.3\hat{i} + 0.4\hat{j})$
(d) $10^2 E_0 \cos [\pi(0.3x + 0.4y - 1000t)](3\hat{i} + 4\hat{j})$

32. The energy of an electron in a band as a function of its wave vector k is given by $E(k) = E_0 - B(\cos k_x a + \cos k_y a + \cos k_z a)$, where E_0, B and a are constants. The effective mass of the electron near the bottom of the band is

- (a) $\frac{2\hbar^2}{3Ba^2}$ (b) $\frac{\hbar^2}{3Ba^2}$
(c) $\frac{\hbar^2}{2Ba^2}$ (d) $\frac{\hbar^2}{Ba^2}$

33. A DC voltage V is applied across a Josephson junction between two superconductors with a phase difference ϕ_0 . If I_0 and k are constants that depend on the properties of the junction, the current flowing through it has the form

- (a) $I_0 \sin \left(\frac{2eVt}{\hbar} + \phi_0 \right)$
(b) $kV \sin \left(\frac{2eVt}{\hbar} + \phi_0 \right)$
(c) $kV \sin \phi_0$
(d) $I_0 \sin \phi_0 + kV$

34. Consider the following ratios of the partial decay widths $R_1 = \frac{\Gamma(\rho^+ \rightarrow \pi^+ + \pi^0)}{\Gamma(\rho^- \rightarrow \pi^- + \pi^0)}$ and $R_2 = \frac{\Gamma(\Delta^{++} \rightarrow \pi^+ + p)}{\Gamma(\Delta^- \rightarrow \pi^- + n)}$. If the effects of electromagnetic and weak interactions are neglected, then R_1 and R_2 are, respectively,

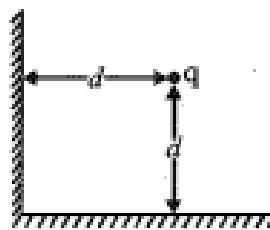
- (a) 1 and $\sqrt{2}$ (b) 1 and 2
(c) 2 and 1 (d) 1 and 1

35. The intrinsic electric dipole moment of a nucleus ${}^A_Z X$
(a) increases with Z , but independent of A
(c) is always zero
(b) decreases with Z , but independent of A
(d) increases with Z and A

36. According to the shell model, the total angular momentum (in units of \hbar) and the parity of the ground state of the ${}^7_3\text{Li}$ nucleus is

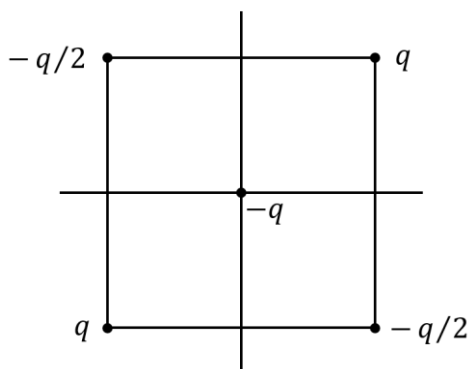
- (a) $\frac{3}{2}$ with negative parity
(b) $\frac{3}{2}$ with positive parity
(c) $\frac{1}{2}$ with positive parity
(d) $\frac{7}{2}$ with negative parity

37. A point charge q is placed symmetrically at a distance d from two perpendicularly placed grounded conducting infinite plates as shown in the figure. The net force on the charge (in units of $1/4\pi\epsilon_0$) is



- (a) $\frac{q^2}{8d^2} (2\sqrt{2} - 1)$ away from the corner
(b) $\frac{q^2}{8d^2} (2\sqrt{2} - 1)$ towards the corner
(c) $\frac{q^2}{2\sqrt{2}d^2}$ towards the corner
(d) $\frac{3q^2}{8d^2}$ away from the corner

38. Let four point charges $q, -q/2, q$ and $-q/2$ be placed at the vertices of a square of side a . Let another point charge $-q$ be placed at the centre of the square (see the figure). Let $V(r)$ be the electrostatic potential at a point P at a distance $r \gg a$ from the centre of the square. Then $V(2r)/V(r)$ is



- (a) 1 (b) $\frac{1}{2}$
(c) $\frac{1}{4}$ (d) $\frac{1}{8}$

39. Let A and B be two vectors in three-dimensional Euclidean space. Under rotation, the tensor product $T_{ig} = A_i B_j$

- (a) reduces to a direct sum of three 3-dimensional representations
(b) is an irreducible 9-dimensional representation
(c) reduces to a direct sum of a 1-dimensional, a 3-dimensional and a 5-dimensional irreducible representations
(d) reduces to a direct sum of a 1-dimensional and an 8-dimensional irreducible representation

40. Fourier transform of the derivative of the Dirac δ -function, namely $\delta'(x)$, is proportional to

- (a) 0 (b) 1
(c) sink (d) ik

41. A particle is in the ground state of an infinite square well potential given by,

$$V(x) = \begin{cases} 0 & \text{for } -a \leq x \leq a \\ \infty & \text{otherwise} \end{cases}$$

The probability to find the particle in the interval between $-\frac{a}{2}$ and $\frac{a}{2}$ is

- (a) $\frac{1}{2}$ (b) $\frac{1}{2} + \frac{1}{\pi}$
(c) $\frac{1}{2} - \frac{1}{\pi}$ (d) $\frac{1}{\pi}$

42. The expectation value of the x-component of the orbital angular momentum L_x in the state $\psi = \frac{1}{5} [3\psi_{2,1,-1} + \sqrt{5}\psi_{2,1,0} - \sqrt{11}\psi_{2,1,+1}]$ (where ψ_{ntm} are the eigenfunctions in usual notation), is

- (a) $-\frac{\hbar\sqrt{10}}{25}(\sqrt{11} - 3)$ (b) 0
(c) $\frac{\hbar\sqrt{10}}{25}(\sqrt{11} + 3)$ (d) $\hbar\sqrt{2}$

43. A particle is prepared in a simultaneous eigenstate of L^2 and L_z . If $\ell(\ell + 1)\hbar^2$ and $m\hbar$ are respectively the eigenvalues of L^2 and L_z , then the expectation value $\langle L_x^2 \rangle$ of the particle in this state satisfies

- (a) $\langle L_x^2 \rangle = 0$
(b) $0 \leq \langle L_x^2 \rangle \leq \ell^2 \hbar^2$
(c) $0 \leq \langle L_x^2 \rangle \leq \frac{\ell(\ell+1)\hbar^2}{3}$
(d) $\frac{\ell\hbar^2}{2} \leq \langle L_x^2 \rangle \leq \frac{\ell(\ell+1)\hbar^2}{2}$

44. If the electrostatic potential $V(r, \theta, \phi)$ in a charge free region has the form $V(r, \theta, \phi) = f(r)\cos \theta$, then the functional form of $f(r)$ (in the following a and b are constants) is

- (a) $ar^2 + \frac{b}{r}$ (b) $ar + \frac{b}{r^2}$
(c) $ar + \frac{b}{r}$ (d) $a \ln \left(\frac{r}{b} \right)$

45. If $\mathbf{A} = \hat{i}yz + \hat{j}xz + \hat{k}xy$, then the integral $\oint_C \mathbf{A} d\mathbf{l}$ (where C is along the perimeter of a rectangular area bounded by $x = 0, x = a$ and $y = 0, y = b$) is

- (a) $\frac{1}{2}(a^3 + b^3)$ (b) $\pi(ab^2 + a^2b)$
(c) $\pi(a^3 + b^3)$ (d) 0

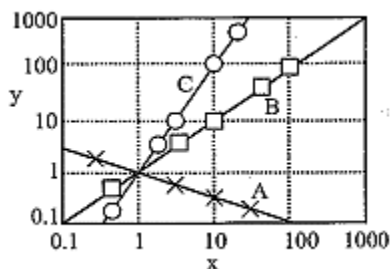
46. Consider an $n \times n$ ($n > 1$) matrix A_a in which A_{ij} is the product of the indices i and j (namely $A_{ij} = ij$). The matrix A

- (a) has one degenerate eigenvalue with degeneracy $(n - 1)$
(b) has two degenerate eigenvalues with degeneracies 2 and $(n - 2)$
(c) has one degenerate eigenvalue with degeneracy n
(d) does not have any degenerate eigenvalue

47. A child makes a random walk on a square lattice of lattice constant a taking a step in the north, east, south, or west directions with probabilities 0.255, 0.255, 0.245, and 0.245, respectively. After a large number of steps, N , the expected position of the child with respect to the starting point is at a distance
- $\sqrt{2} \times 10^{-2} Na$ in the north-east direction
 - $\sqrt{2N} \times 10^{-2} a$ in the north-east direction
 - $2\sqrt{2} \times 10^{-2} Na$ in the south-east direction
 - 0

48. A Carnot cycle operates as a heat engine between two bodies of equal heat capacity until their temperatures become equal. If the initial temperatures of the bodies are T_1 and T_2 , respectively, and $T_1 > T_2$ then their common final temperature is
- T_1^2/T_2
 - T_2^2/T_1
 - $\sqrt{T_1 T_2}$
 - $\frac{1}{2}(T_1 + T_2)$

49. Three sets of data A , B and C from an experiment, represented by \times , \square and O , are plotted on a log-log scale. Each of these are fitted with straight lines as shown in the figure.



The functional dependence $y(x)$ for the sets A , B and C are, respectively

- \sqrt{x} , x and x^2
- $-\frac{x}{2}$, x and $2x$
- $\frac{1}{x^2}$, x and x^2
- $\frac{1}{\sqrt{x}}$, x and x^2

50. A sample of Si has electron and hole mobilities of 0.13 and 0.05 $\text{m}^2/\text{V-s}$ respectively at 300 K. It is doped with P and Al with doping densities of $1.5 \times 10^{21}/\text{m}^3$ and $2.5 \times 10^{21}/\text{m}^3$ respectively. The

conductivity of the doped Si sample at 300 K is

- $8\Omega^{-1}\text{m}^{-1}$
- $32\Omega^{-1}\text{m}^{-1}$
- $20.8\Omega^{-1}\text{m}^{-1}$
- $83.2\Omega^{-1}\text{m}^{-1}$

51. A 4-variable switching function is given by $f = \Sigma(5,7,8,10,13,15) + d(0,1,2)$, where d is the donot-care-condition. The minimized form of f in sum of products (SOP) form is
- $\bar{A}\bar{C} + \bar{B}\bar{D}$
 - $A\bar{B} + C\bar{D}$
 - $AD + BC$
 - $\bar{B}\bar{D} + BD$

52. A perturbation $V_{\text{pert}} = a L^2$ is added to the Hydrogen atom potential. The shift in the energy level of the 2P state, when the effects of spin are neglected up to second order in a , is
- 0
 - $2a\hbar^2 + a^2\hbar^4$
 - $2a\hbar^2$
 - $a\hbar^2 + \frac{3}{2}a^2\hbar^4$

53. A gas laser cavity has been designed to operate at $\lambda = 0.5\mu\text{m}$ with a cavity length of 1 m. With this set-up, the frequency is found to be larger than the desired frequency by 100 Hz. The change in the effective length of the cavity required to retune the laser is
- $-0.334 \times 10^{-12} \text{ m}$
 - $0.334 \times 10^{-12} \text{ m}$
 - $0.167 \times 10^{-12} \text{ m}$
 - $-0.167 \times 10^{-12} \text{ m}$

54. The spectroscopic symbol for the ground state of ^{13}Al is $^2P_{1/2}$. Under the action of a strong magnetic field (when L-S coupling can be neglected) the ground state energy level will split into

- 3 levels
- 4 levels
- 5 levels
- 6 levels

55. A uniform linear monoatomic chain is modeled by a spring-mass system of masses m separated by nearest neighbor distance a and spring constant $m\omega_0^2$. The dispersion relation for this system is

- $\omega(k) = 2\omega_0 \left(1 - \cos\left(\frac{ka}{2}\right)\right)$

$$(b) \omega(k) = 2\omega_0 \sin^2 \left(\frac{ka}{2} \right)$$

$$(c) \omega(k) = 2\omega_0 \sin \left(\frac{ka}{2} \right)$$

$$(d) \omega(k) = 2\omega_0 \tan \left(\frac{ka}{2} \right)$$

❖ ANSWER KEY

1-c	2-b	3-a	4-d	5-d
6-d	7-d	8-a	9-b	10-b
11-a	12-b	13-d	14-b	15-c
16-c	17-d	18-c	19-a	20-c
21-b	22-b	23-c	24-d	25-c
26-c	27-c	28-a	29-a	30-d
31-b	32-d	33-a	34-d	35-c
36-a	37-b	38-d	39-c	40-d
41-b	42-a	43-d	44-b	45-d
46-a	47-a	48-c	49-d	50-a
51-d	52-c	53-d	54-d	55-c

